Supplement for Paper “A Multilingual Topic Model for Learning Weighted Topic Links Across Corpora with Low Comparability”

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A Generative Details of our Multilingual Topic Model

Our MTM is a downstream model with a posterior regularizer. It has two LDA components that generate the documents in languages $S$ and $T$. Then it generates the posterior regularizer $\Psi$ which encodes the cross-lingual knowledge. The detailed generative process is as follows.

1. For each topic $k \in \{1, \ldots, K_T\}$ in language $T$
   (a) Draw word distribution $\phi_{T,k} \sim \text{Dirichlet}(\beta_T)$.

2. For each document $d \in \{1, \ldots, D_T\}$ in language $T$
   (a) Draw topic distribution $\theta_{T,d} \sim \text{Dirichlet}(\alpha_T)$.
   (b) For each token $t_{T,d,n}$ in document $d$
      i. Draw a topic $z_{T,d,n} \sim \text{Multinomial}(\theta_{T,d})$.
      ii. Draw a word $w_{T,d,n} \sim \text{Multinomial}(\phi_{T,z_{T,d,n}})$.

3. For each topic $k \in \{1, \ldots, K_S\}$ in language $S$
   (a) Draw word distribution $\phi_{S,k} \sim \text{Dirichlet}(\beta_S)$.

4. For each document $d \in \{1, \ldots, D_S\}$ in language $S$
   (a) Draw topic distribution $\theta_{S,d} \sim \text{Dirichlet}(\alpha_S)$.
   (b) For each token $t_{S,d,n}$ in document $d$
      i. Draw a topic $z_{S,d,n} \sim \text{Multinomial}(\theta_{S,d})$.
      ii. Draw a word $w_{S,d,n} \sim \text{Multinomial}(\phi_{S,z_{S,d,n}})$.

5. Draw the posterior regularizer $\Psi = \left(\prod_{c=1}^{C} \| \Omega_{S,c} - \rho_{T \rightarrow S} \Omega_{T,c} \|_2^{\eta_c} \| \rho_{S \rightarrow T} \Omega_{S,c} - \Omega_{T,c} \|_2^{\eta_c}\right)^{-1}$.

A.1 Posterior Inference

As we mentioned in the paper, the posterior inference is based on stochastic EM and consists of an E-step and an M-step [1]. In each iteration, the E-step updates every token’s topic assignment using Gibbs sampling, while holding the values in the topic link weight matrices $\rho$. The M-step optimizes $\rho$ while holding the topic assignments.

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A.1.1 E-Step: Topic Assignment Sampling

In addition to the usual word and topic dependencies, our MTM encourages topic assignments that maximize the posterior regularizer \( \Psi \), thus make the related translation pairs’ (transformed) topic distributions close. This is reflected in the Gibbs sampling equation to update \( z_{T,d,n} \), the topic assignment of the \( n \)-th token of document \( d \) in language \( T \):

\[
\Pr(z_{T,d,n} = k \mid z_{-T,d,n}, w_{T,d,n} = v, w_{-T,d,n}, \rho, \alpha_T, \beta_T) \propto \left( \frac{N_{T,d,n} - T_{d,k} + \alpha_T}{N_{T,d,n} + \alpha_T} \right)^{\frac{N_{T,d,n} - T_{d,k} + \beta_T}{N_{T,d,n} + V_T + \beta_T}} \]

where the first two terms are the same as LDA: \( N_{T,d,k} \) denotes the number of tokens in document \( d \) assigned to topic \( k \); \( N_{S,k,v} \) denotes the number of times word \( v \) is assigned to topic \( k \); \( \cdot \) denotes marginal counts; \( z_{-T,d,n} \) means the count excludes the token. The final term corresponds to the posterior regularizer: \( \text{Dic}(v) \) is word \( v \)’s translation word set in language \( S \); The values of \( \Omega_{v,v} \), the topic distribution of word \( v \), assume topic \( k \) is chosen as follows:

\[
\Omega_{T,v,k} = \frac{N_{T,d,n} - T_{d,k} + \mathbb{1}(k' = k)}{N_{T,d,n}},
\]

where \( \mathbb{1}(\cdot) \) is an indicator function.

Symmetrically, the Gibbs sampling equation to update \( z_{S,d,n} \), the topic assignment of the \( n \)-th token of document \( d \) in language \( S \), is

\[
\Pr(z_{S,d,n} = k \mid z_{-S,d,n}, w_{S,d,n} = v, w_{-S,d,n}, \rho, \alpha_S, \beta_S) \propto \left( \frac{N_{S,d,n} - S_{d,k} + \alpha_S}{N_{S,d,n} + \alpha_S} \right)^{\frac{N_{S,d,n} - S_{d,k} + \beta_S}{N_{S,d,n} + V_S + \beta_S}} \]

\[
\left( \prod_{v' \in \text{Dic}(v)} \left\| \Omega_{S,v'} - \rho_{T \rightarrow S} \Omega_{T,v'} \right\|_2^{\frac{n_{v,v'}}{\eta_{v,v'}}} \right)^{-1}. \]

The values of \( \Omega_{S,v} \), assuming topic \( k \) is chosen, are

\[
\Omega_{S,v,k} = \frac{N_{S,d,n} - S_{d,k,v} + \mathbb{1}(k' = k)}{N_{S,d,n}}. \]

A.1.2 M-Step: Parameter Optimization

Here we optimize the topic link weight matrices \( \rho \) while fixing the topic assignments. As \( \Psi \) is the product over all translation pairs, we modify \( \Psi \) to obtain the objective functions \( J(\rho_{T \rightarrow S}) \) and \( J(\rho_{S \rightarrow T}) \) as the weighted logarithmic sum\(^1\)

\[
J(\rho_{T \rightarrow S}) = \sum_{c=1}^{C} \eta_c \log \left\| \Omega_{S,c} - \rho_{T \rightarrow S,i_S} \Omega_{T,c} \right\|_2
\]

\[
J(\rho_{S \rightarrow T}) = \sum_{c=1}^{C} \eta_c \log \left\| \Omega_{T,c} - \rho_{S \rightarrow T,i_T} \Omega_{S,c} \right\|_2.
\]

\(^1\)It makes sense to add regularization on \( \rho \)’s to prevent overfitting, but the data already adds a strong constraint on \( \rho \)’s—each word’s \( \Omega \) values should add up to one.
The objective functions are then minimized by using L-BFGS [2] and the partial derivatives with respect to $\rho_{T \rightarrow S, k_S, k_T}$ and $\rho_{S \rightarrow T, k_T, k_S}$ as

$$\frac{\partial J}{\partial \rho_{T \rightarrow S}} = - \sum_{c=1}^{C} \eta_c \left( \frac{\Omega_{T,c,k_T} - \rho_{T \rightarrow S, k_S} \Omega_{T,c}}{\| \Omega_{S,c} - \rho_{T \rightarrow S, i_S} \Omega_{T,c} \|^2} \right)$$

(7)

$$\frac{\partial J}{\partial \rho_{S \rightarrow T}} = - \sum_{c=1}^{C} \eta_c \left( \frac{\Omega_{S,c,k_S} - \rho_{S \rightarrow T, k_T} \Omega_{S,c}}{\| \Omega_{T,c,k_T} - \rho_{S \rightarrow T, i_T} \Omega_{S,c} \|^2} \right)$$

(8)

B Corpora Statistics

There are four datasets used in our experiments. The first one is collected from Wikipedia for document category classification in English (EN) and Chinese (ZH) [3]. There are six document categories for Wikipedia documents: film, music, animals, politics, religion, and food. The dictionary comes from MDBG, a website for learning Chinese.²

The second dataset is about disaster response in English and Sinhalese (SI) [4, 5]. A subset of the documents are annotated with one of eight need types: evacuation, food supply, search/rescue, utilities, infrastructure, medical assistance, shelter, and water supply. The dictionary is provided by the dataset authors.

The last two are also collected from Wikipedia, one is partially comparable (PACO) and the other one is incomparable (INCO) [6]. Either one contains five bilingual corpora. Among these bilingual corpora, one of the language is always English (EN), while the other language is one of Arabic (AR), Chinese (ZH), Spanish (ES), Farsi (FA), and Russian (RU). The dictionaries are extracted from Wiktionary.³

The detailed corpora statistics are in Table 1.

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Table 1: Corpora Statistics.

²https://www.mdbg.net/chinese/dictionary?page=cc-cedict
³https://dumps.wikimedia.org/enwiktionary/
C An Example of Topic Space Transformation with Top-Linked Topics

We give an example to illustrate how we transform topic space with top-linked topics. Suppose that we have a Chinese topic with a probability mass of 0.2 in a document and its topic link weight to English Topics 0–4 are 0.1, 0.4, 0.2, 0.1, 0.2. Given that English Topic 1 has the highest link weight with the Chinese topic, when transforming the document’s topic distribution into English, the probability mass of the Chinese topic is transferred to English Topic 1.

References


